ST. THOMAS SCHOOL WORKSHEET-4 CLASS-IX (MATHEMATICS)

1. Express the following in the form of $\frac{p}{q}$, where p and q are integers and q $\neq 0$

2. Without actually calculating the cubes, find the value of

$$\left(\frac{-3}{4}\right)^3 + \left(\frac{-5}{8}\right)^3 + \left(\frac{11}{8}\right)^3$$

- **3.** In a class number of girls is x that of boys is y. Also the number of girls is 10 more than the number of boys. Write the given data in the form of a linear equation in two variables. Also represent it graphically. Find graphically the number of girls, if the number of boys is 20.
- 4. Draw the graph of equations 2x + 3y = -5 and x + y = -1 in the same graph. Find the co-ordinates of the point of intersection of two lines.
- 5. Write the co-ordinates of the vertices of a rectangle whose length and breadth are 8 and 5 units respectively. One vertex at (1, 0), the longer side lies on the x-axis and one of the vertices lies in the second quadrant.
- 6. A cloth having an area of 165m² is shaped into the form of a conical tent of radius 5cm.
 - i) How many students can sit in the tent if a student on an average occupies $\frac{5}{7}$ m²on the ground?
 - ii) Find the volume of the cone.
- 7. The surface area of a sphere of radius 5 cm is five times the curved surface area of a cone of radius 4 cm. Find the height and volume of the cone.
- 8. Ten observations 6, 14, 15, 17, x + 1, 2x 13, 30, 32, 34, 43 are written in an ascending order. The median of the data is 24. Find the value of x.
- 9. The mean of five numbers is 15. If one number is excluded, their mean remains 15. Find the excluded number.
- 10. Mean of 25 observations was found to be 40.4 .But later on, it was discovered that 53 was misread as 35 at one place. Find the correct mean.
- 11. Draw a histogram and frequency polygon on the same graph for the following distribution:

| Marks | 0-10 | 10 - 20 | 20 – 30 | 30 – 40 | 40 – 50 | 50 –60 | 60 - 70 | 70 - 80 |
|----------|------|---------|---------|---------|---------|--------|---------|---------|
| No of | 7 | 10 | 6 | 8 | 12 | 3 | 2 | 2 |
| Students | | | | | | | | |

12. If the mean of the following data is 20.2, find the value of p.

| х | 10 | 15 | 20 | 25 | 30 |
|---|----|----|----|----|----|
| f | 6 | 8 | р | 10 | 6 |

13. A teak wood log is cut first in the form of cuboid of length 2.3m, width 75cm and of certain thickness. Find its thickness, if its volume is 1.104m³. How many rectangular planks of size 2.3m x 75cm x 4cm can be cut from the cuboid?

- 14. Simplify: $\sqrt[4]{81}$ -8 ($\sqrt[3]{216}$) +15 ($\sqrt[5]{32}$) + $\sqrt{225}$.
- 15. Prove that the sum of three angles of a triangle is 180° .
- 16. Solve using suitable identities. i) $1000^3 - 999^3$ ii) 99^3 iii) $(2x - 3)^3$ iv) $(2x - 3y + z)^2$
- 17. Find the value of a and b so that (x + 1) and (x 1) are factors of $x^4+ax^3+2x^2-3x+b$.
- 18. If $x = \frac{\sqrt{2} + 1}{\sqrt{2} 1}$ and $y = \frac{\sqrt{2} 1}{\sqrt{2} + 1}$, find the value of $x^2 + y^2 + xy$.
- 19. Plot the points A(0,3),B(5,3),C(4,0) and D(-1,0) on the graph paper. Identify the figure ABCD and find whether the points E(2,2) lies inside the figure or not?
- 20. AB and CD are two parallel lines intersected by transversal EF. Bisectors of interior angles BPQ and DQP intersect at R. Prove that ∠PRQ = 90∘

